

# **Performance of Coherent Doppler Lidar for General Space-Based Conditions with Pulse Accumulation**

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**Support for GTWS Coherent Lidar Simulation**

# DEFINITION OF LOS VELOCITY ACCURACY

- **Velocity field is random**
- **Definition of velocity accuracy requires definition of truth " $v_{\text{truth}}$ "**
- **Accuracy composed of bias and random error  $e$**

$$\hat{v} = v_{\text{truth}} + e + \text{BIAS}$$

- **Bias of estimate =  $\langle \hat{v} - v_{\text{truth}} \rangle$**   
 **$\langle x \rangle$  denotes ensemble average of  $x$**
- **Random error  $\sigma^2 = \langle [\hat{v} - \langle \hat{v} \rangle]^2 \rangle$**
- **Definition of truth depends on application**

## **SPACE-BASED VELOCITY ESTIMATE: FIXED STARE WITH PULSE ACCUMULATION**

- **True velocity is the average of the LOS velocity over the measurement plane**
- **"Good" estimates have a Gaussian PDF with standard deviation  $\sigma$  (random error)**
- **"Good" estimates are unbiased if backscatter is uncorrelated with the LOS velocity**
- **Random error is typically dominated by effects of wind turbulence and backscatter variability**
- **"Bad" estimates described by the fraction  $b$  of uniformly distributed estimates**
- **Threshold signal level determined by fraction of "bad" estimates**

# LARGE NUMBER OF INPUT PARAMETERS

- $\lambda$  - laser wavelength (1.5 - 10.1  $\mu\text{m}$ )
- $\Delta t$  - pulse width (0.2-2.0  $\mu\text{sec}$  FWHM)
- $\Delta r$  - pulse target extent (30-300 m FWHM)
- $\Delta p$  - range-gate length (250-2000 m)
- $\sigma_{\text{turb}}$  - radial velocity fluctuations from turbulence
- $\sigma_{\text{vLO}}$  - shot-to-shot uncorrelated instrumental radial velocity error
- $\beta$  - backscatter statistics  
(mean, spatial correlation, PDF)
- $V_{\text{search}}$  - velocity search space (10-100 m/s)
- $V_{\text{shear}}$  - velocity shear (0-50 m/s/km)
- $U$  - pulse energy
- $A$  - telescope aperture
- PRF - pulse repetition frequency
- L - pulse accumulation track length

# EFFECTIVE GAUSSIAN SIGNAL SPECTRUM MODEL

- simplifies analysis with four parameters
- $\Phi_1$  - effective photons per LOS range-gate
- M - number of data samples per LOS range-gate
- N - pulse accumulation
- $\Omega$  - effective normalized spectral width

$$\Omega = 2 w_v M T_s / \lambda$$

$w_v$  - spectral width in velocity space

- valid for the weak to moderate signal regime
- simple scaling laws for threshold signal level  $\Phi_1^K$

CAPON  $\lambda=2.0 \mu\text{m}$   $\tau=0.5 \mu\text{sec}$  (FWHM)  $v_{\text{search}}=20.0 \text{ m/s}$   $M=150$

A

$\Delta r=75.00 \text{ m}$   $\Delta p=1125.00 \text{ m}$   $\Omega_{\text{eff}}=11.2422$  zenith angle= $45.0^\circ$

$\sigma_h=1.7861 \text{ m/s}$   $\sigma_v=1.2630 \text{ m/s}$   $\sigma_{vLO}=0.5 \text{ m/s}$

$\varepsilon=2.66e-5 \text{ m}^2/\text{s}^3$   $L_{0h}=200.0 \text{ km}$   $s_v=1.4513 \text{ m/s}$   $w_v=1.4990 \text{ m/s}$

shots=100 track length=100.000 km shot separation=1.0 km

shear=5.0 m/s/km  $L_{0\beta}=200.0 \text{ km}$   $\sigma_\beta/\beta=1.0$

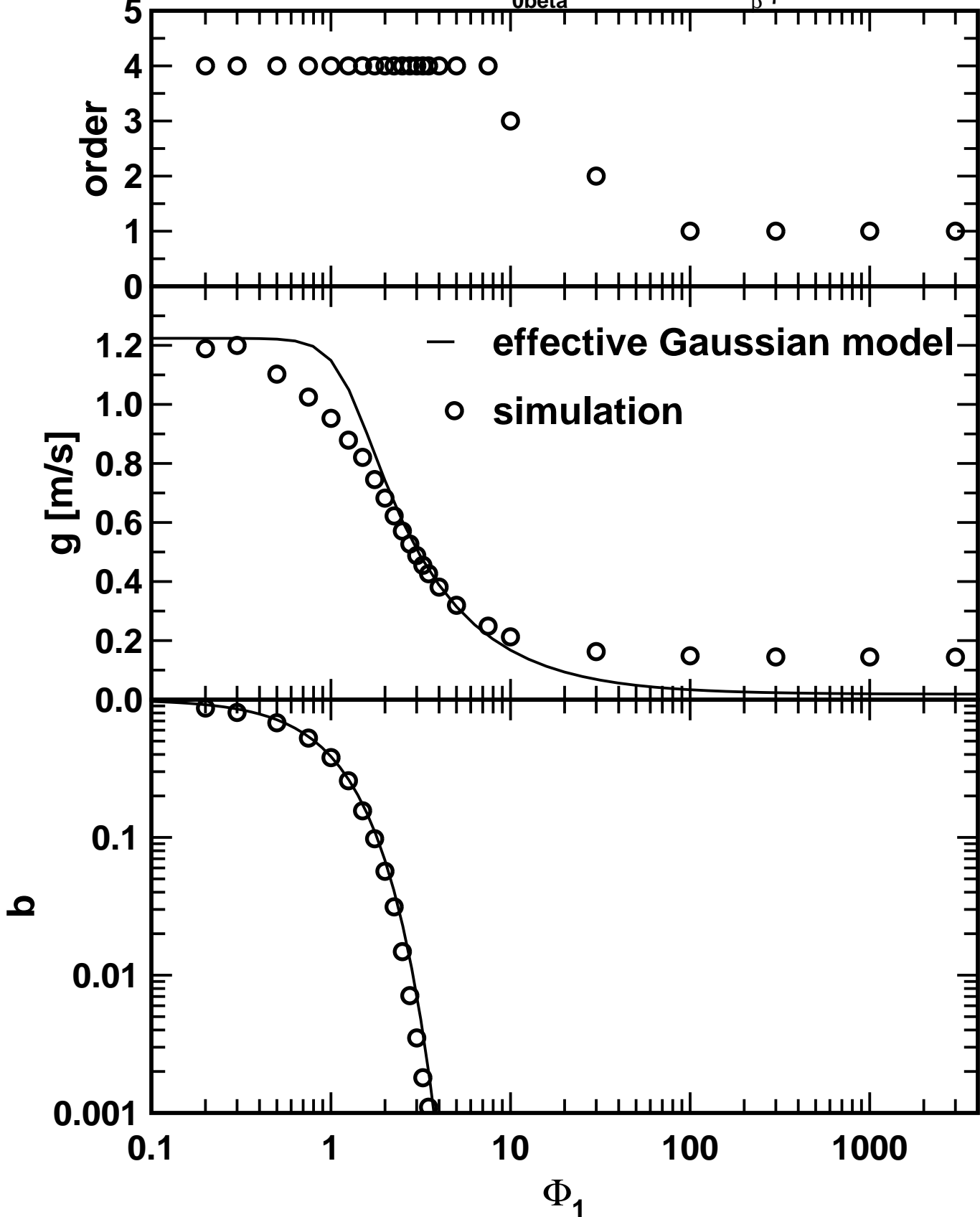


Figure 15 Frehlich, JTech, Vol. 13, 646-658, 1996

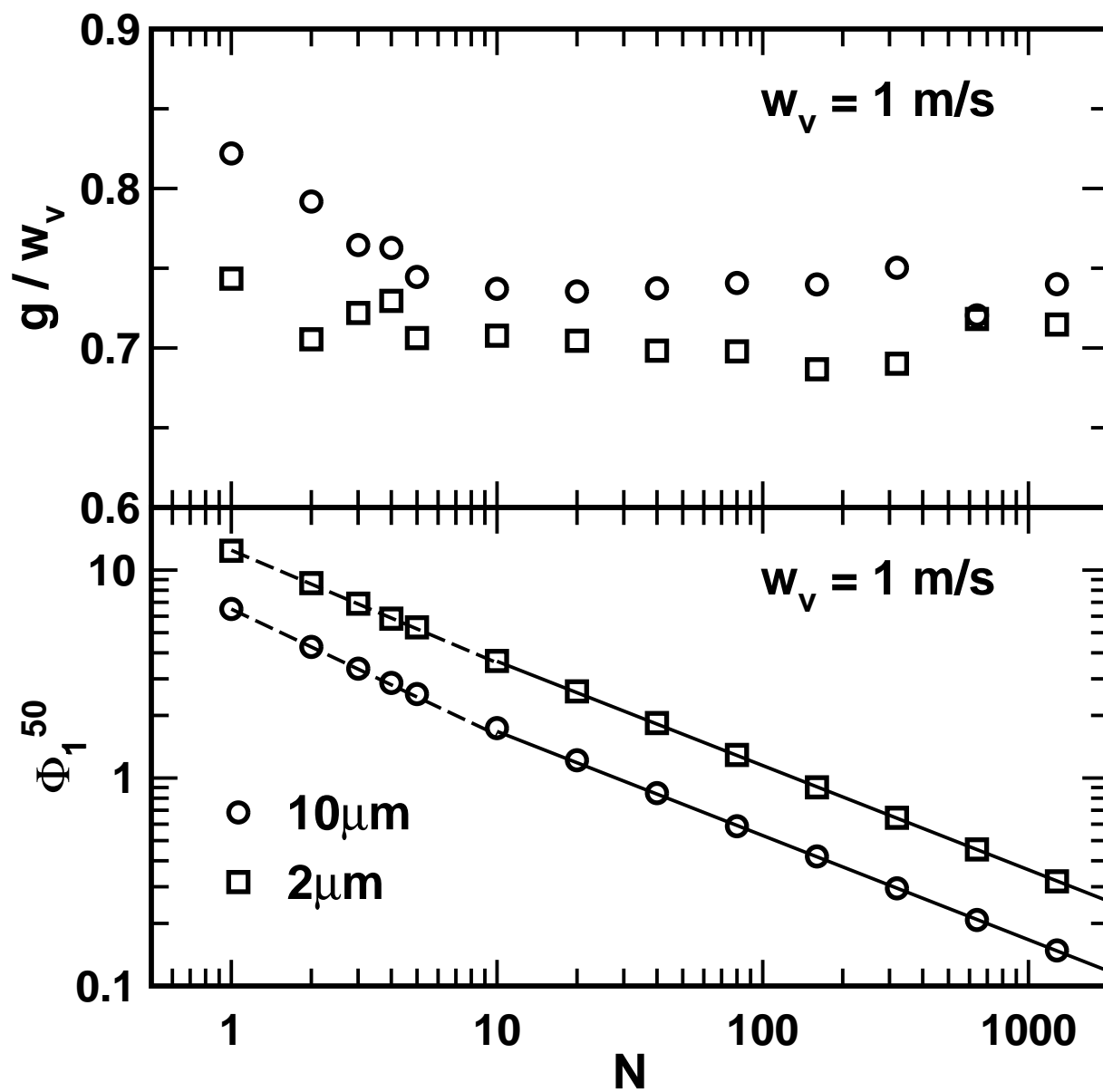


Figure 16 Frehlich, JTech, Vol. 13, 646-658, 1996

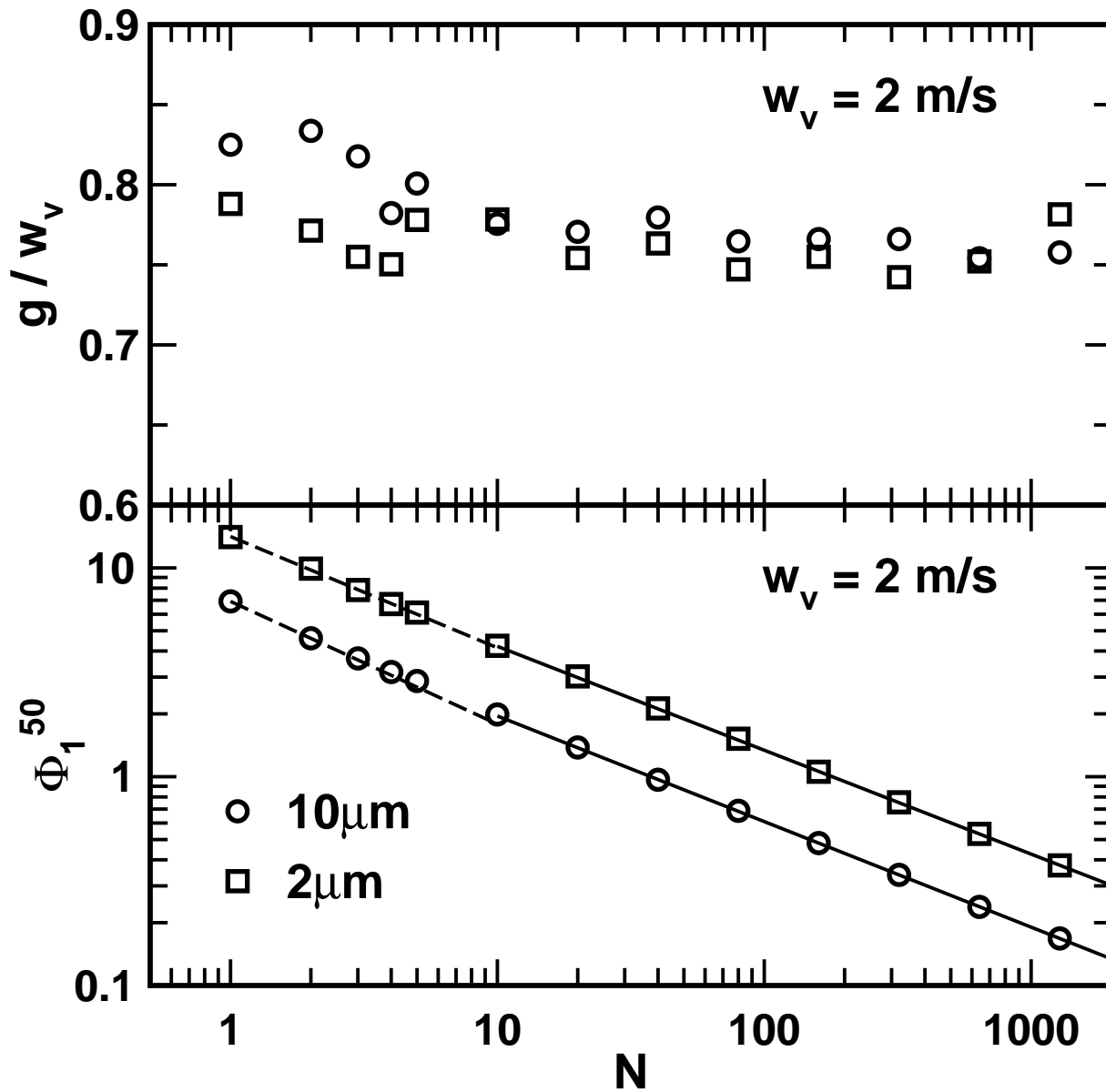




Figure 17 Frehlich, JTech, Vol. 13, 646-658, 1996

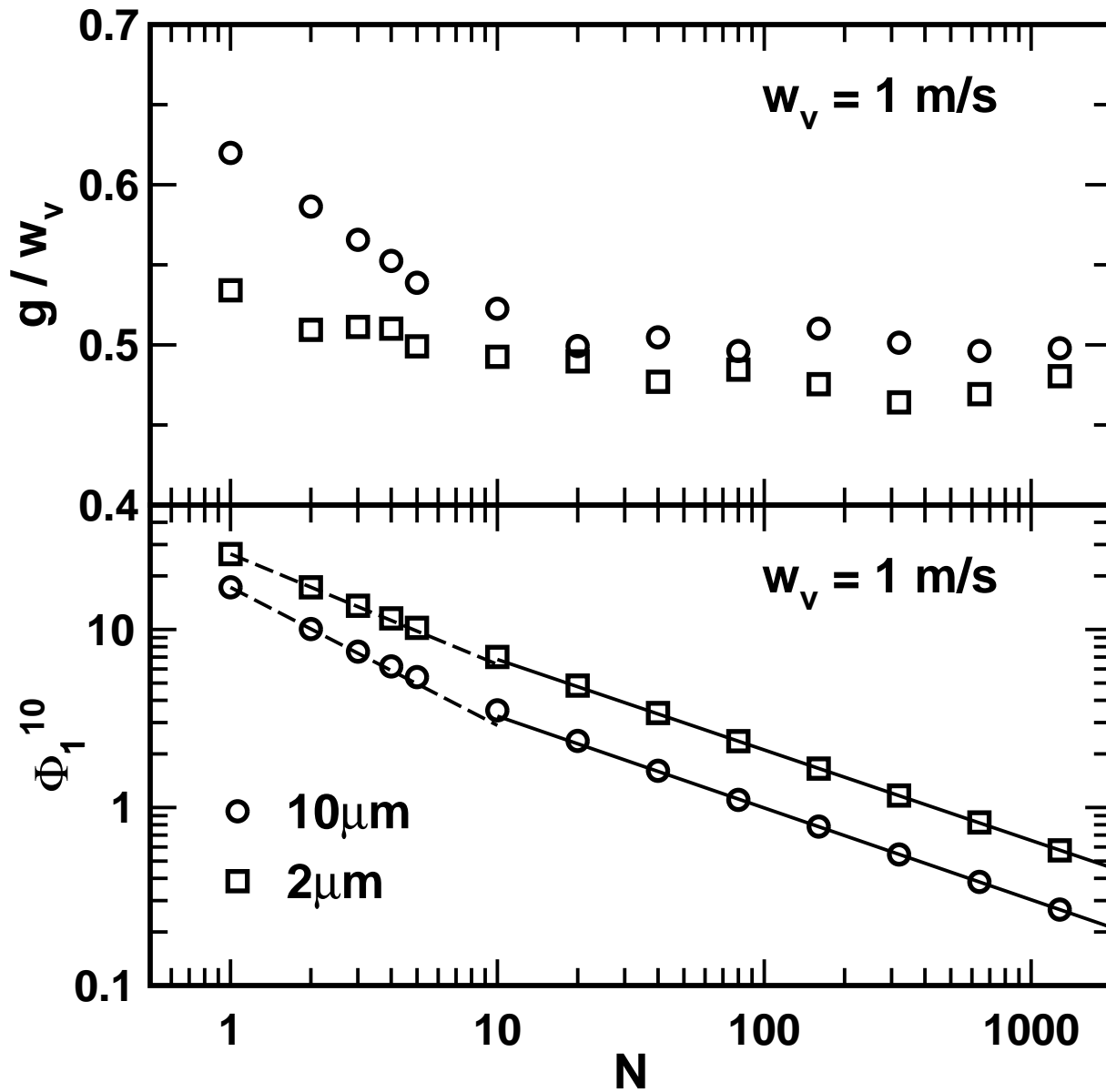


Figure 18 Frehlich, JTech, Vol. 13, 646-658, 1996

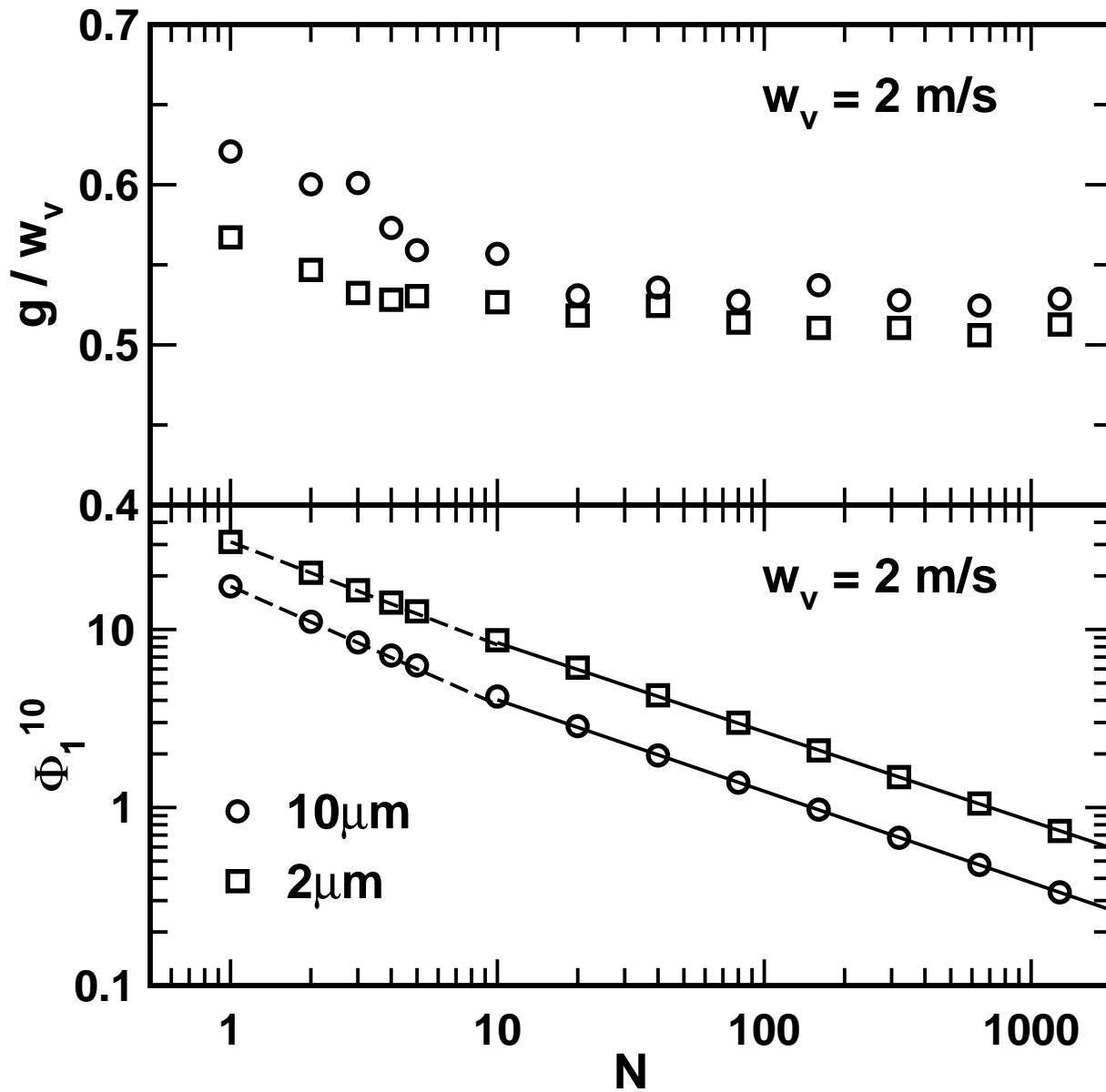
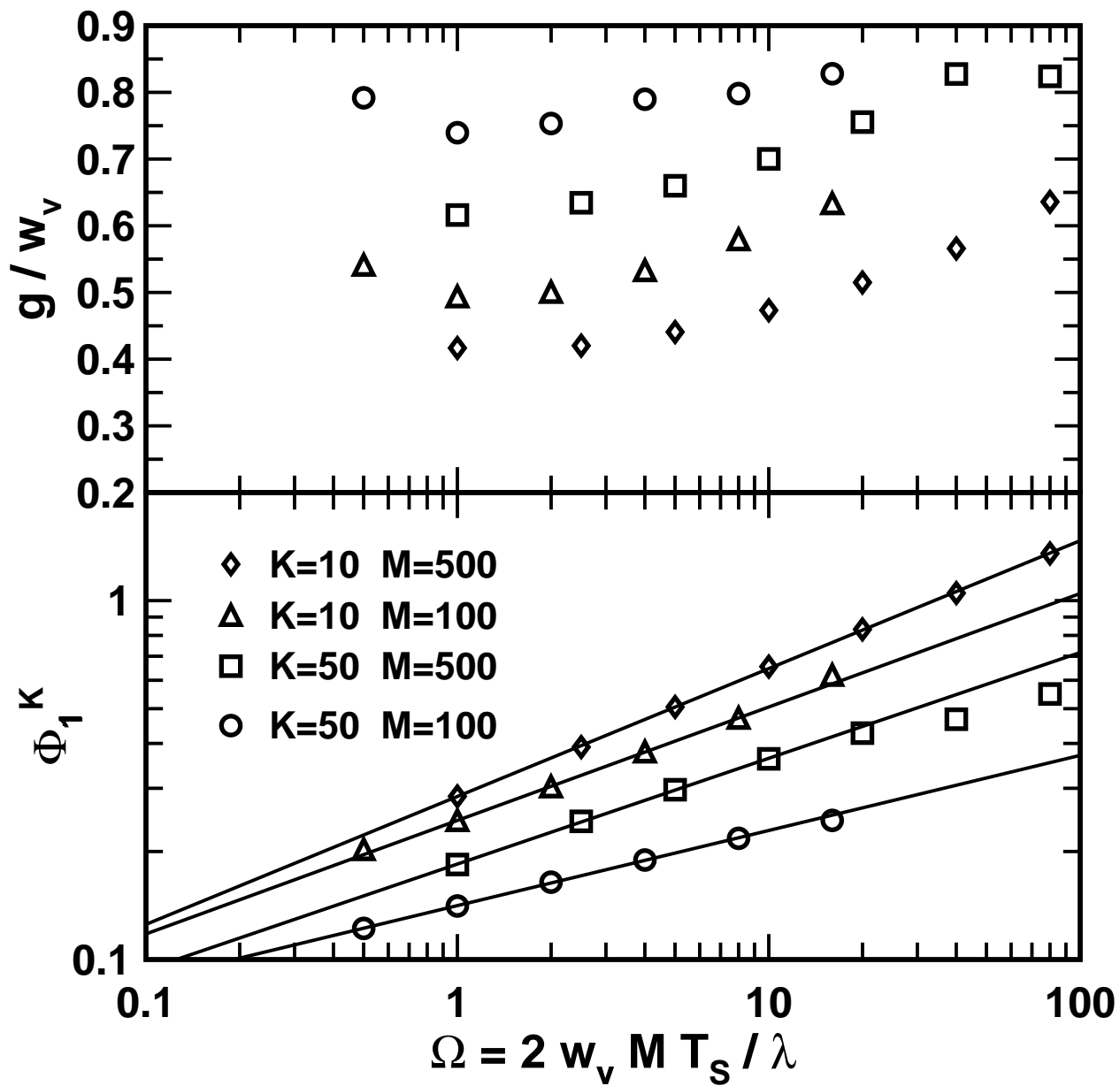


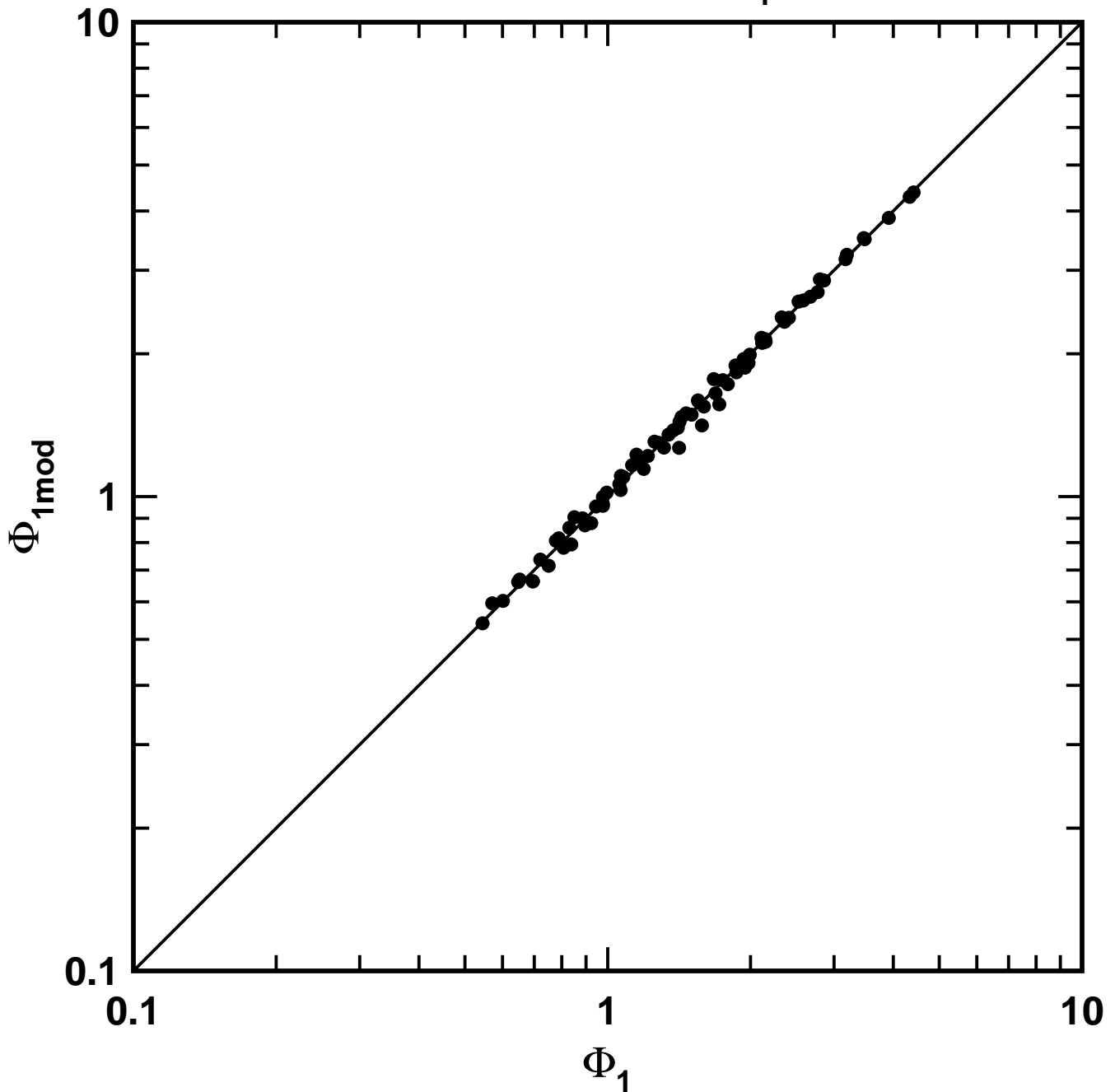
Figure 19 Frehlich, JTech, Vol. 13, 646-658, 1996



$$\Phi_{1\text{mod}}(M,\Omega,N,b)=4.708201 N^{-0.528988} M^{0.148501} \Omega^{0.289007}$$

average percent error=3.330  $b_{\text{min}}=0.005$   $b_{\text{max}}=0.4$

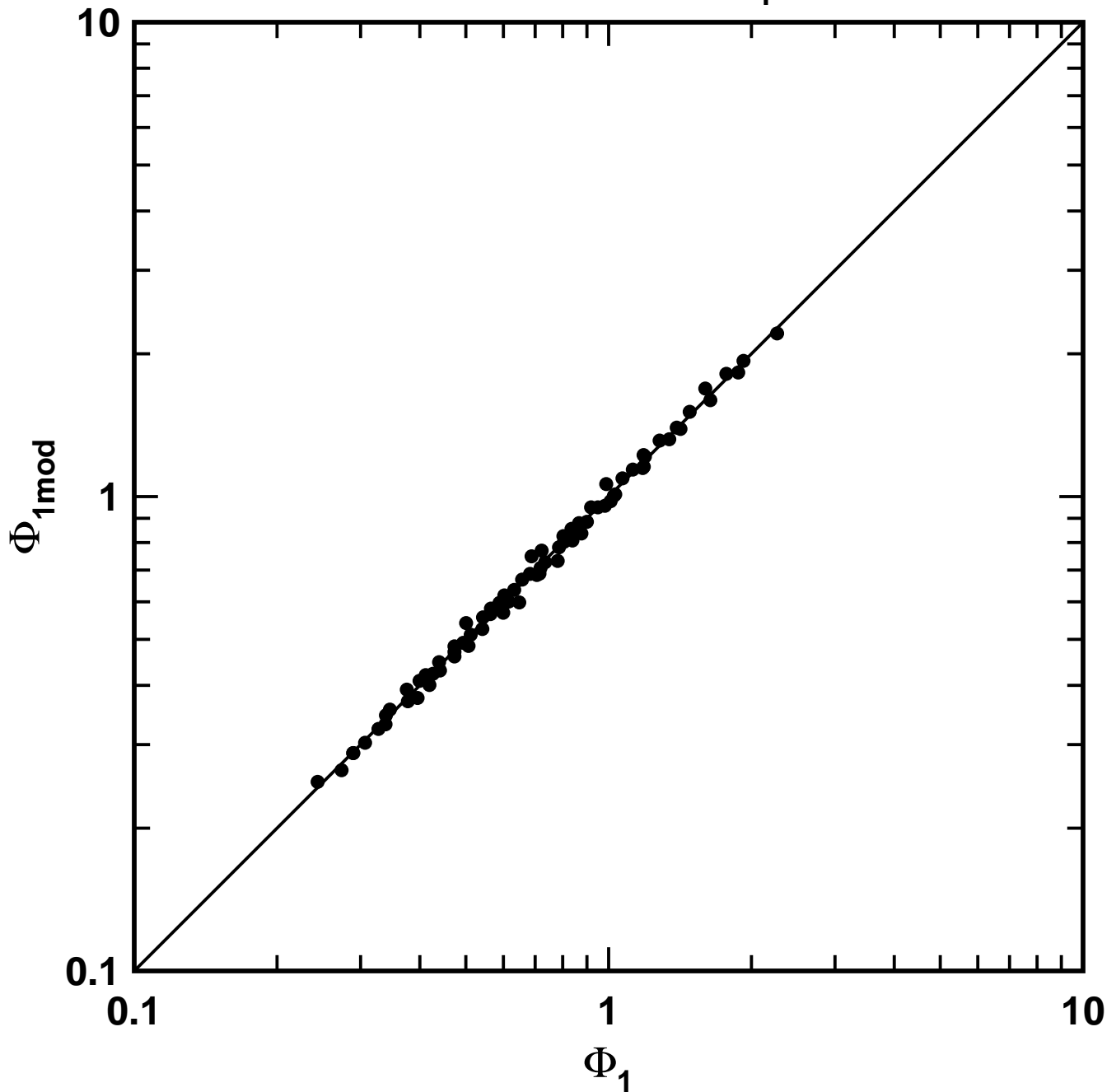
threshold single shot  $\Phi_1$  at  $b=0.1$



$$\Phi_{1\text{mod}}(M,\Omega,N,b)=1.304073 N^{-0.506371} M^{0.274183} \Omega^{0.192710}$$

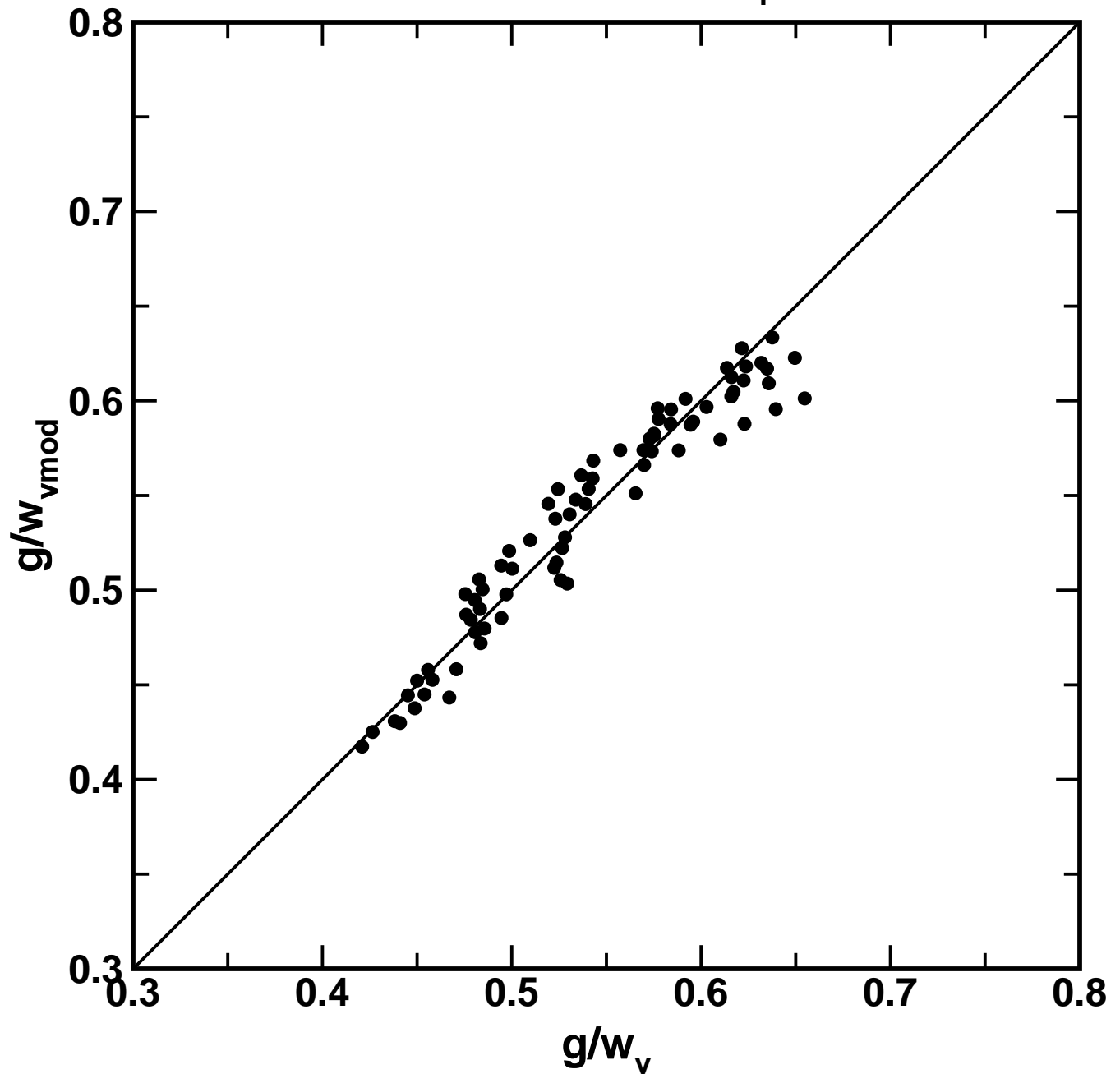
average percent error=3.211  $b_{\text{min}}=0.05$   $b_{\text{max}}=0.8$

threshold single shot  $\Phi_1$  at  $b=0.5$



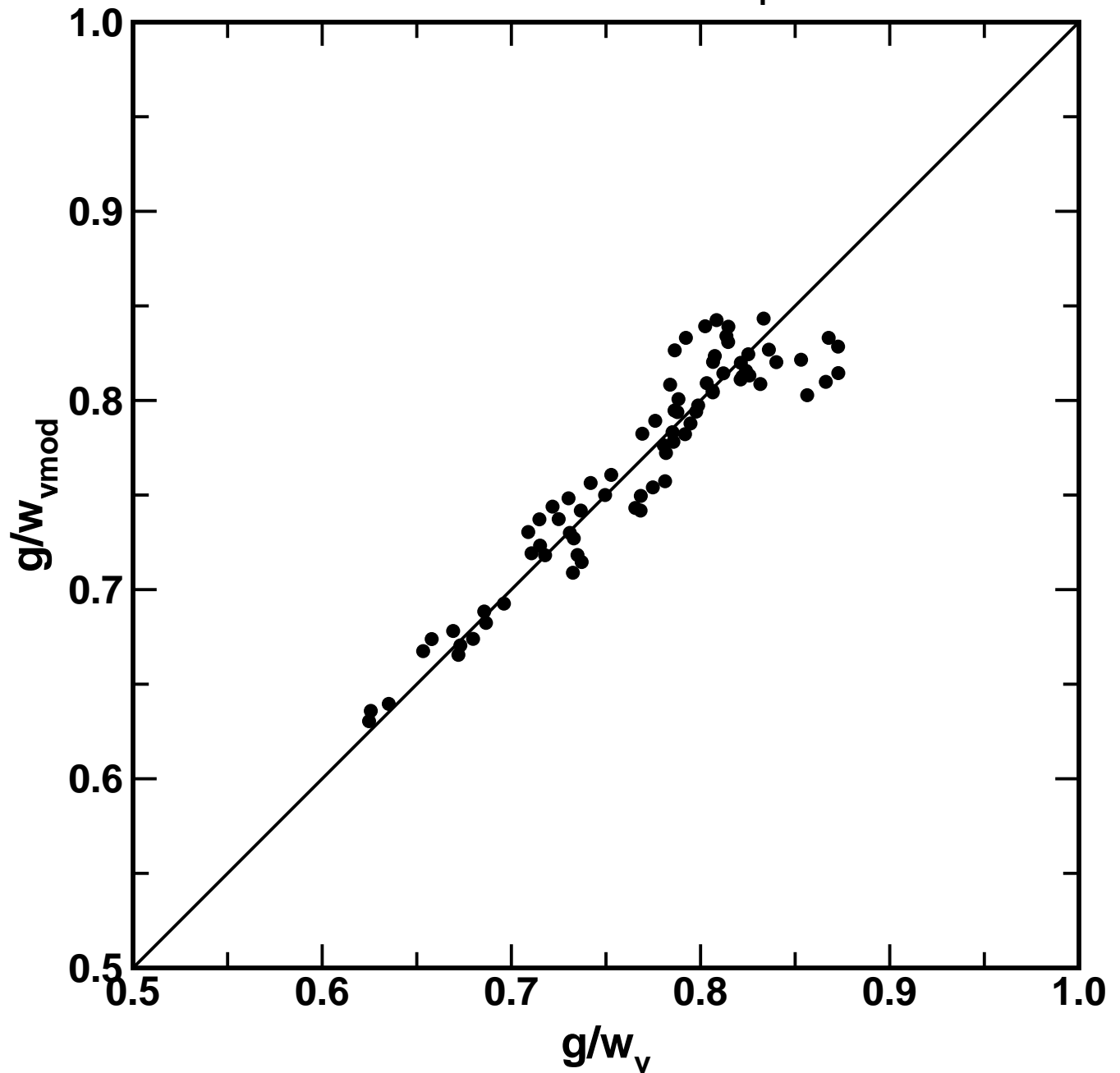
average percent error=2.911  $b_{\min}=0.005$   $b_{\max}=0.4$

threshold single shot  $\Phi_1$  at  $b=0.1$



average percent error=2.495  $b_{\min}=0.05$   $b_{\max}=0.8$

threshold single shot  $\Phi_1$  at  $b=0.5$



## **SUMMARY**

- **Performance in threshold region described by four basic parameters**
- **Simple scaling laws for threshold signal level and LOS velocity error at threshold**
- **Full parameter space must be investigated**
- **Determine atmospheric conditions for validity of the effective Gaussian signal model**
- **Spatial velocity and backscatter statistics over the measurement plane are required**
- **Hope to incorporate general performance predictions in GTWS modeling efforts**