Horizontal Mixing in the WRF-ARW Model

Russ Schumacher AT 730 5 April 2006

Overview

 Description of implicit and explicit horizontal mixing in WRF

- Evaluation of WRF's implicit mixing
- Model options for explicit mixing & filters
- 2D and 3D Smagorinsky schemes

Introduction

- Most mesoscale models use a turbulence closure scheme to represent subgrid-scale effects – these schemes are based in part on turbulence theory and observations
- As we learned in our HW assignment, finite-difference advection schemes also introduce computational errors, especially at small scales
- To remove these small-scale perturbations, additional artificial mixing is sometimes added (usually via a scale-selective spatial filter)
- Artificial filters are necessary in models with centered-in-space advection, but artificial filters for diffusion are not standard nor necessary in WRF (some have experimented with their use, however)
- WRF does use artificial filters for acoustic and external modes

Implicit mixing in WRF

- The 3rd-order Runge-Kutta (RK3) time integration scheme used in WRF can be used stably with high-order approximations to the advection equation
- If an odd-ordered advection approximation is used, the RK3 scheme has a built-in filter of the next-highest order
 - If using 5th-order advection approximation, a 6th-order filter is included
- The implicit filter damps small-scale oscillations with a coefficient proportional to the Courant number (C/60 for the 5th-order advection scheme)
- Therefore, WRF can be run without explicit mixing (i.e., no turbulence scheme) this is recommended for $\Delta x > 10$ km
- However, turbulence closure schemes are also an option in WRF and are generally used for higher-resolution applications (NWP, cloud modeling, etc.)

Evaluation of WRF implicit mixing

- Skamarock (2004) found that the energy spectra produced by WRF compare well with the observed k⁻³ and k^{-5/3} spectra
- He defines the "effective resolution" of a model to be the point at which the model spectrum is damped relative to the correct spectrum
- The tailing-off at high wavenumbers is necessary to avoid energy buildup and unphysical behavior at very small scales
- However, it's undesirable to overdamp physical small-scale features (otherwise, there would be no reason to use smaller grid spacing)





Evaluation of WRF implicit mixing

- The implicit 6th-order filter in WRF-ARW, compared with explicit filters used in other NWP models, is the most scale selective and the least dissipative
- This means that it only dissipates at the highest wavenumbers, which increases the "effective resolution" of the model
- Skamarock (2004) found WRF's effective resolution to be ~7Δx, compared with ~10Δx for other NWP models
- He suggests that this might be nearing the limit for effective resolution





Options for explicit mixing

Diffusion options:

- No explicit mixing
- Diffusion evaluated on model coordinate (eta) surfaces
- Diffusion evaluated in physical (x,y,z) space using stress & deformation tensors

Options for computation of eddy viscosities (km_opt):

- **1:** Constant K_h and K_v (specified by user)
- **2:** 1.5 order prognostic TKE closure
- **3:** 3D first-order Smagorinsky closure
- 4: Horizontal first-order Smagorinsky closure
- If a PBL parameterization is employed, it handles all vertical mixing: all other explicit vertical mixing is disabled (options 1 or 4 are recommended in this case)

Coordinate vs. physical space

- If mixing is done on coordinate surfaces, K_h is allowed to vary in space, but K_v is not
- Since coordinate surfaces follow terrain, the "horizontal" diffusion can introduce vertical diffusion in areas with sloping terrain
- Coordinate-surface diffusion can only be used with km_opt = 1 or 4 (constant K or 2D Smagorinsky)
- For physical-space diffusion, coordinate metrics are computed at each time step using the geopotential:

 $z_x = g^{-1} \delta_x \varphi ; z_y = g^{-1} \overline{\delta_y \varphi}$

Stress and deformation tensors are calculated in a method similar to that described in Ch. 6 of the book

2D Smagorinsky scheme

Recall that first-order turbulence closure can be represented using eddy viscosity coefficients:

$$\overline{w''\theta''} = -K_{\theta} \frac{\partial \bar{\theta}}{\partial z}, \qquad \overline{w''q_k''} = -K_{\theta} \frac{\partial \bar{q}_k}{\partial z}, \qquad \overline{w''\chi_m''} - K_{\theta} \frac{\partial \overline{\chi}_m}{\partial z},$$
$$\overline{w''u''} = -K_m \frac{\partial \bar{u}}{\partial z}, \qquad \text{and} \qquad \overline{w''v''} = -K_m \frac{\partial \bar{v}}{\partial z},$$

- We then need to calculate the values of K (in WRF K_h and K_v)
- The 2D Smagorinsky scheme calculates only K_h -- it is most often used when a PBL scheme is handling the vertical mixing independently
- It uses the horizontal deformation to calculate K_h, which in WRF is shown by:

$$K_h = C_s^2 \, l^2 \bigg[0.25 (D_{11} - D_{22})^2 + \overline{D_{12}^2}^{xy} \bigg]^{\frac{1}{2}}.$$

 $C_s = \text{constant} (\text{typically 0.25})$ $l = \text{length scale} (\Delta x \Delta y)^{1/2}$ D terms represent deformation For scalars, K_h divided by Pr =1/3

3D Smagorinsky scheme

- This scheme is similar to the 2D scheme but also includes vertical mixing (used without PBL scheme – mainly for idealized simulations)
- Depends on horizontal and vertical deformation and stability
- Kh and Kv determined by:

$$K_{h,v} = C_s^2 \, l_{h,v}^2 \max\left[0., D^2 - \left(P_r^{-1} N^2\right)^{1/2}\right],$$

where

$$D = \frac{1}{2} \left[D_{11}^2 + D_{22}^2 + D_{33}^2 \right] + \left(\overline{D_{12}}^{xy} \right)^2 + \left(\overline{D_{13}}^{x\eta} \right)^2 + \left(\overline{D_{23}}^{y\eta} \right)^2,$$

 $C_s = constant (typically 0.25)$ D terms represent deformation N = Brunt-Vaisala frequency Pr = Turbulent Prandtl number For scalars, K divided by Pr =1/3

User specifies critical length scale: if Δx is less than this length, then $l_h = l_v = (\Delta x \Delta y \Delta z)^{1/3}$ and $K_h = K_v$; if greater, $l_h = (\Delta x \Delta y)^{1/2}$ and $l_v = \Delta z$

Summary and conclusions

The advection scheme used in WRF includes an implicit scale-selective filter – the model can be run stably without a turbulence closure scheme and without artificial mixing

- This implicit filter is found to increase the effective resolution of the model it does not overdamp small-scale perturbations
- WRF provides several options for turbulence closure, one of which is usually used when performing high-resolution simulations